

# Modeling of Partial Discharge Mechanisms in Solid Dielectric Material

Y. Z. Arief, W. A. Izzati, Z. Adzis

**Abstract**— *Partial discharge (PD) represents a physical phenomenon, in which discharges are involved in electrically weak regions of solid insulation materials (mostly within gaseous or liquid inclusions). They cause damage to the insulation and often start from the enclosed voids and/or at interface defects. The period in which the insulation is still in good operating condition is of great practical interest. The effect of PD also results in failure of the dielectric much before the expected life-time. This project was conducted by simulations based on an extended PD equivalent circuit in order to understand the characteristics of PD in solid dielectric materials. In this project, PD mechanism in solid dielectric material was modeled using Simulink in MATLAB®. This project focused on the results of the partial discharges in solid dielectric with a single cavity as defect. AC source with 50Hz frequency voltage was applied. It is observed that the discharge current is proportional with the input voltage. The discharge current amplitude for input 10 kV is half the input of 20 kV and a third of 30 kV input. All discharge currents and discharge voltages occur in nano-seconds.*

**Index Terms**—Partial Discharge, Extended PD Equivalent Circuit, Modeling of Partial Discharge, Solid Dielectric.

## I. INTRODUCTION

Partial discharge (PD) is defined as localized electrical discharge within only a part of the insulation between two separated conductors. In the real applications, PD is caused by the existence of voids in the insulation. Even if the local electrical field in the void exceeds a threshold and a discharge occurs, it is limited within the void due to the strong surrounding insulation, enough to avoid a complete breakdown. PD in voids is considered harmful, especially in high-voltage systems from the engineering viewpoint as they cause energy loss and gradually degrade the insulation [1].

PD may occur in solid, liquid and gaseous insulation media and are generally initiated by an excessive localized electric field. The PD induced current in an external circuit depends on the nature of the discharge and the geometry of the system [2]. In many cases, where there are electrically weak areas in solid dielectric materials (most often gaseous or liquid inclusions), PD can be measured when enough voltage is applied. PD phenomenon causes degradation in insulated materials. The investigation of insulated material behaviour under electrical stress and the data obtained from PD measurements, provide the possibility to predict dielectric breakdown. There are three main types of PD: (i) micro discharges in small voids, which always exist both at the surface of electrodes and in the volume of insulators; (ii)

breakdowns along the boundaries between two insulators (typically along the solid insulator–gas interface); and (iii) PD in the channels of branched structures (streamers) propagating in the volume of a dielectric medium. The second and third PD types can be considered as incomplete breakdown, since the insulating properties of a dielectric are not violated. The most complete information is provided by the so-called “phase resolved data,” which have been determined for PD of all types in numerous experimental investigations [3]. Some PD simulation results which related with this work have been reported during this decade [4-9].

Fig. 1 shows an ideal PD pulse. The pulse is characterized by rise time ( $T_r$ ), decay time ( $T_d$ ), and pulse width ( $T_w$ ). Pulse rise time ( $T_r$ ), is the time required to rise from 10% to 90% levels of the peak pulse value; pulse decay time ( $T_d$ ), is the time required to decay from 90% to 10% levels of the peak pulse value; whereas pulse width ( $T_w$ ), is the time interval between 50% levels on both sides of the peak pulse value.

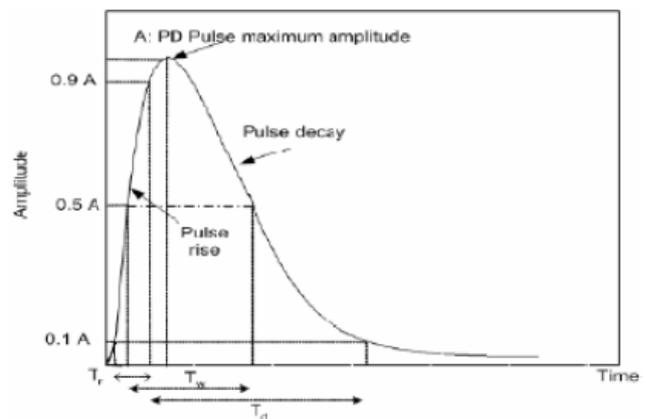


Fig. 1. Parametric characterization of PD pulse [10].

PD behaviour in inclusions (cavities, defects, etc.) in dielectrics can be represented by simple equivalent circuit developed by Gemant & Philippoff in 1932 [10], known as capacitance model. A dielectric with an internal void is shown schematically in Fig. 2, where:

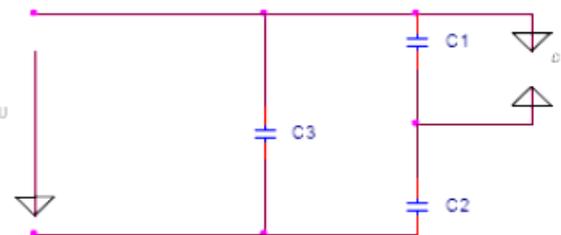


Fig. 2. Equivalent circuit of partial discharge

- U : applied voltage at power frequency,
- C<sub>1</sub> : capacitor representing the cavity,
- C<sub>2</sub> : capacitor representing insulating material around cavity,
- C<sub>3</sub> : capacitance of the remaining insulating material,
- S : spark gap representing discharge of C<sub>1</sub>.
- C<sub>1</sub> and C<sub>2</sub> are generally not measurable.

However, the capacitance model can lead to quite incorrect conclusions, because it does not take into account the influence of all the relevant void parameters. In considering the additional electric field generated by the preceding discharge, an improved equivalent circuit has to be used. Circuit models that represent PD behavior have been developed long ago. A lot of improved circuit models have been established by researchers to get better understanding on PD. Old circuit models did not consider the role of space charges, but it can be solved by improvements to the equivalent circuit.

This project aims to simulate a circuit model of PD mechanisms in solid dielectric material utilizing MATLAB<sup>®</sup> software version 7.0.0.19920 (R14). The characteristics of PD in solid dielectric material were studied from the simulation results. This simulation involved the extended equivalent circuit based on Gemant & Philippoff's capacitance model.

**II. MODELING OF PARTIAL DISCHARGE IN VOIDS**

Modelling is used in this research in highlighting some of the techniques that have been used, modified, and proposed in an effort to come out with a meaningful contribution to PD analysis and interpretation. For some discharge phenomena, physical models have been developed by researchers such as Brunt, 1991 and Neimeyer, 1995. However, until now little work has been accomplished to formulate a generalized and theoretical framework to describe the PD stochastic phenomenon. By far, computer simulation programs and models for PD are scarce commodities in research. Hence, integrated models such as the one pursued in this research have not been fully realized by previous researchers, due to the complexity of the PD process. Heitz (1999) has suggested that until then there is often a severe mismatch between very sophisticated measuring facilities on one hand and strong difficulty in interpretation of the measured PD data on the other hand. Progress has recently been made by Hoof and Patsch (1998) who developed a model which is valid for different defect types. However the model was later criticized by Wu (2004), who suggested that conventional methods such as these, assumes a purely deterministic discharge behaviour and cannot be used for situations where the inherent stochastic properties of the PD generation are relevant.

Wu (2004) specifically referred to the conventional method of phase – resolve PD pattern (i.e. -q-n pattern, q: phase angle, and n: PD number) as an ineffective approach to

disclose the PD mechanism. Reference was also made to the Monte Carlo simulation of the phase-resolved PD pattern. This conventional method of simulation, assumed that the total field in a cavity after PD, is reduced in proportion to the PD magnitude, and that the critical field for PD occurrence and the residual field after the discharge, mainly determine the subsequent PD magnitude. These kinds of models are thought to be inefficient in describing the large difference among PD magnitudes in cavities, in insulating materials, and the implications of changes in PD pattern with degradation.

The PD process can be considered as defined by a sequence of electrical discharges under the influence of an externally applied field E<sub>0</sub>(t). The discharges (PD events) lead to a charge deployment in the vicinity of the PD defect which initiate a so called internal field E<sub>i</sub>(t). Each PD event changes the internal field suddenly. Between the successive PD events, the internal field changes due to charge dissipation mechanism like surface conduction in voids, or charge carrier drift in gas discharges. The dynamics of the process can be described briefly in the following.

During a discharge at time t the total electric field E<sub>tot</sub>(t),

$$E_{tot} = E_o(t) + E_i(t) \tag{1}$$

Drops to a residual filed E<sub>res</sub> :

$$E_{tot} \rightarrow E'(t) = \pm E_{res} \tag{2}$$

**III. PHYSICAL MODEL**

Based on experimental investigations of PD resulting from various insulation defects, a model has been developed that involves only three physically meaningful parameters. A PD occurs if the electric strength within a certain region of the insulation of an electric device is locally exceeded, but the surrounding insulation is strong enough to avoid a total breakdown. Hence the local discharge inception field is a relevant parameter. Resulting from the charge separation during a PD, local space or surface charges q, prevents the PD by producing an electric field, ΔE opposite to the ignition field, E<sub>i</sub>. This prevents resignation until a change of the external voltage and/or a decay of the local charge again lead to an electric field, E<sub>i</sub>, which exceeds the local inception field, E<sub>i</sub>.

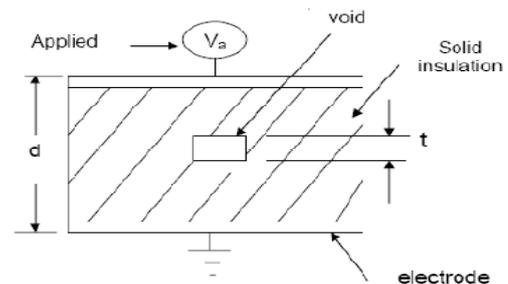


Fig. 3. Physical Modeling of a Void in Polymeric Cables [11].

As long as the defect is not changed by the influence of the PD, the numerical value of the inception field  $E_i$  where the local breakdown occurs neither will be changed. After a corresponding change of the externally applied voltage  $u$  another PD will occur. The fundamental correlations are shown in Fig. 3. The local field  $E_i$  before discharge  $n+1$  is given by equation (3).

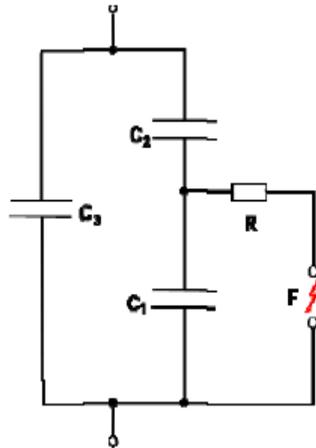


Fig. 4. Conventional PD circuit [10].

Consequently, along with the inception field, the numerical values of the field resets  $\Delta E_q$  due to charge carriers being moved in the PD and a characteristic decay time  $\tau$  for their dissipation and/or recombination are two other important parameters. The parameter  $\Delta E_q$  is determined by residual charges from preceding discharges. As with all physical quantities, there is a certain scatter in the numerical values of the parameters, which has to be included in the simulations.

$$E_i(t_{n+1}) = \hat{E} \sin(\omega t_{n+1}) + [\Delta E_q + \Delta E^\pm] \exp\left(-\frac{t_{n+1} - t_n}{\tau_q^\pm}\right) \quad (3)$$

It is obvious that geometrically non symmetric discharge paths behave different for both polarities of the applied voltage. Hence, there will be different numerical values of the three parameters for different polarities. The important point in the model is the decoupling of the magnitude of the local electric field from the externally applied voltage. Therefore the phase angle of the applied voltage cannot be taken as a meaningful parameter as can be seen in Fig. 6 [10].

#### IV. SIMULATION

The PD circuit that has been used in this project came from a conventional circuit proposed by Gemant & Philippoff in 1932. The circuit is also known as 3 Capacitance Model as shown in Fig. 4. The model was then reconstructed in order to consider the additional electric field generated by preceding discharges, as can be seen in Fig. 5.

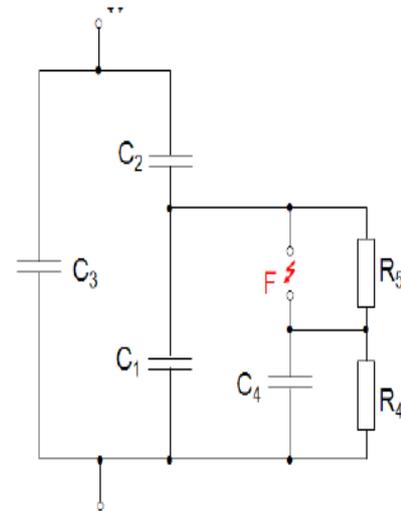


Fig. 5. Extended PD equivalent circuit [10]

Where:

- F : spark gap,
- $C_1$  : capacitance of defect (void, impulse),
- $C_2$  : capacitance of the healthy series with the defect,
- $C_3$  : parallel capacitance in specimen, and
- $C_4$  : capacitance of local charges accumulation.

$$Q = \frac{C_1 C_2}{C_1 + C_2} \times \frac{C_4}{C_1 + C_4} \times (U_1 - U_4) \quad (4)$$

$$U_F = U_1 - U_4 \quad (5)$$

The capacitor  $C_4$  is charged from the capacitor  $C_1$  during the PD process until the two voltages are equal. A consecutive discharge occurs only if the voltage in equation (5) reaches the ignition voltage  $U_F$  of the spark gap. This may happen by a change of  $U_1$  by the external voltage or by a change of  $U_4$  (via a discharging process over  $R_4$ ) or by both. The value of components in the circuit for the simulation is described in Table 1. This circuit was implemented with Simulink application in MATLAB® software. The spark gap in the Fig. 5 has been changed with the breaker in simulation circuit as shown in Fig. 7. This breaker is set with certain time value to represent PD occurring time.

The circuit developed in Simulink application in MATLAB® for the experiment is shown in Fig. 8. Scope 1 is used to observe discharge current, Scope 2 is to observe voltage discharge waveform and Scope 3 is to observe input voltage. In the simulation the solver solves initial value problems for ordinary differential equations (ODEs). Different solver can solve with different accuracy. We chose ode23tb with low accuracy to solve the stiff problem. The algorithms used in the ODE solvers vary according to the order of accuracy [11] and type of systems (stiff or non-stiff) they are designed to solve.

Table 1. Value Of Circuit Component In AC Source For Simulation

AC Vin(kV) 50Hz		10
		15
		20
		30
Rin		5kΩ
C1		10pF
C2		20pF
C3		15pF
C4		1pF
R4		10kΩ
R5		5kΩ
Breaker Timing (second)	Open	1/60
	Close	1/55

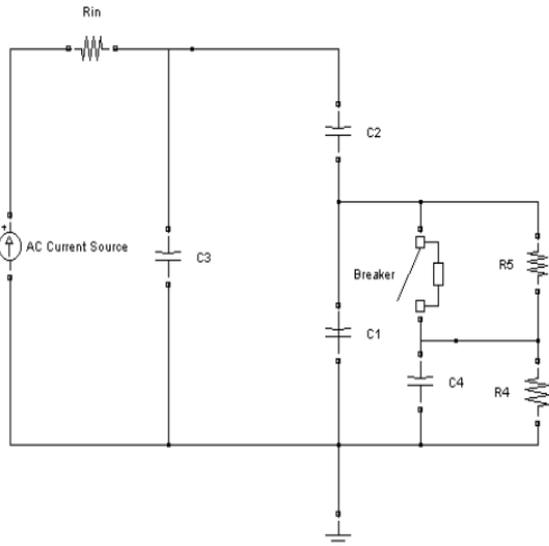
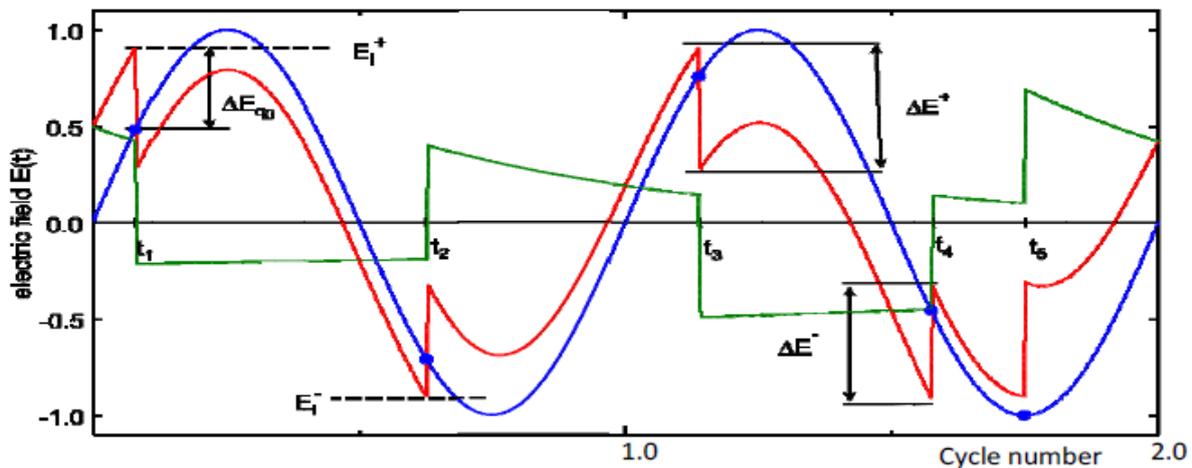


Fig. 6 Simulation Of PD Circuit With AC Source in Simulink.



- electric field  $E_0(t)$  according to external voltage  $u(t)$
- $E_1(t) = E_0(t) + \Delta E_q(t)$ ;  $\tau_q^- = 0.5$  cycles;  $\tau_q^+ = 5$  cycles
- electric field  $\Delta E_q(t)$  according to space charges

Fig. 7. Physical Model for the Simulation [10].

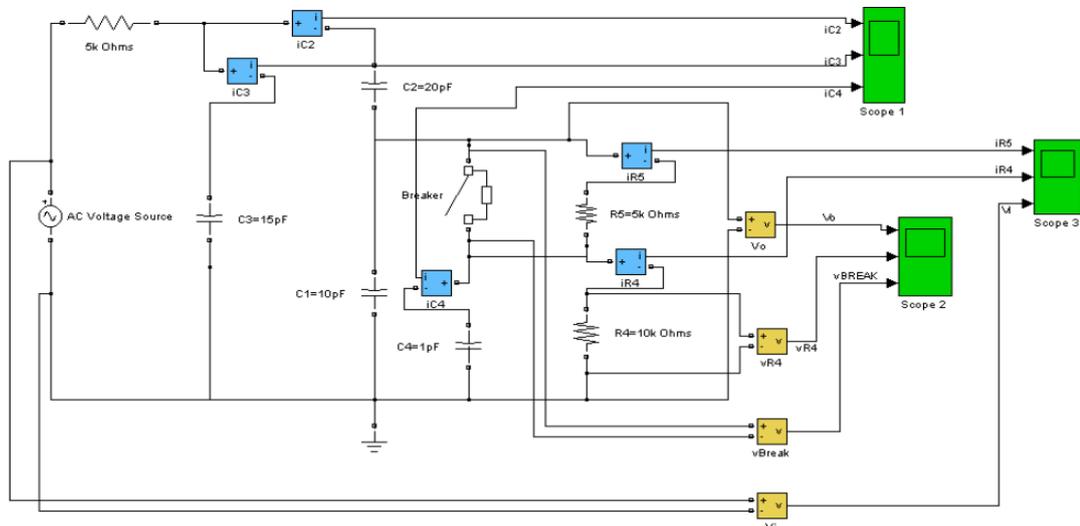


Fig. 8. Simulated Circuit Established in Simulink

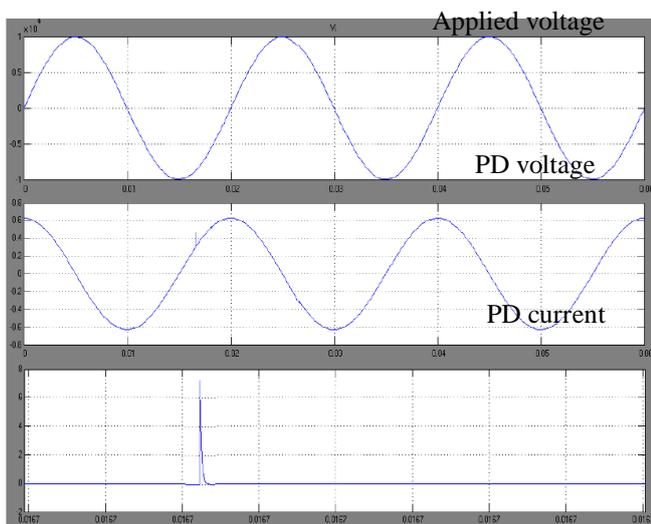
**V. RESULTS AND DISCUSSION**

The simulation was run for 0.06 second. The applied voltage frequency was set to 50 Hz. The results of the simulation are shown in Figs. 9 to 12 for each applied voltage (10, 15, 20, and 30 kV respectively) which were observed from Scope 1 to 3, respectively (arranged in vertical order from top to bottom). From the results, discharges vary at every input voltage. For an increasing AC source, the amplitude of waveform in sampling resistance increased, as well as the single discharges waveform in a void. We observed that the discharge current is proportional with the input voltage, as can be seen in Table 2. The discharge current amplitude for input 10 kV is half of 20 kV input and a third of 30 kV input. All discharge currents and discharge voltages occurred in nano-seconds. The discharge occurred

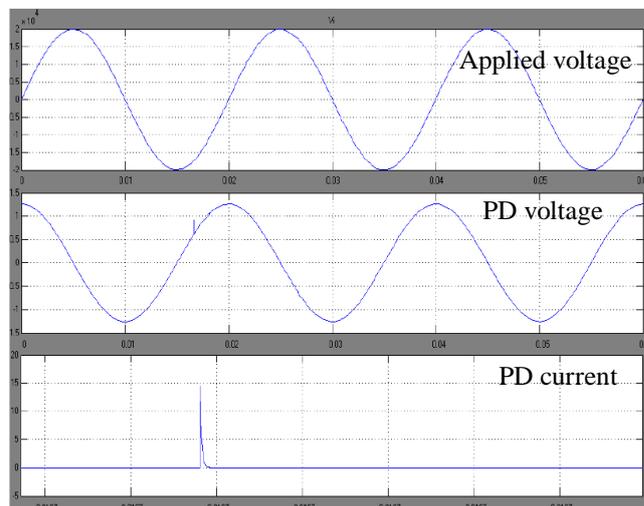
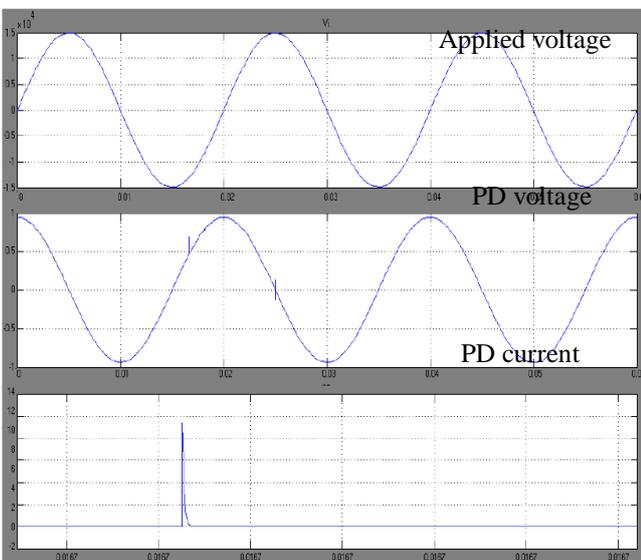
once because of the non repetitive switching mode of the breaker. To make the switching more frequent, it is necessary to replace the breaker with a circuit appropriate for repetitive switching.

**Table 2. Current Discharges in 1 Decimal Places Corresponding With Applied Input Voltage**

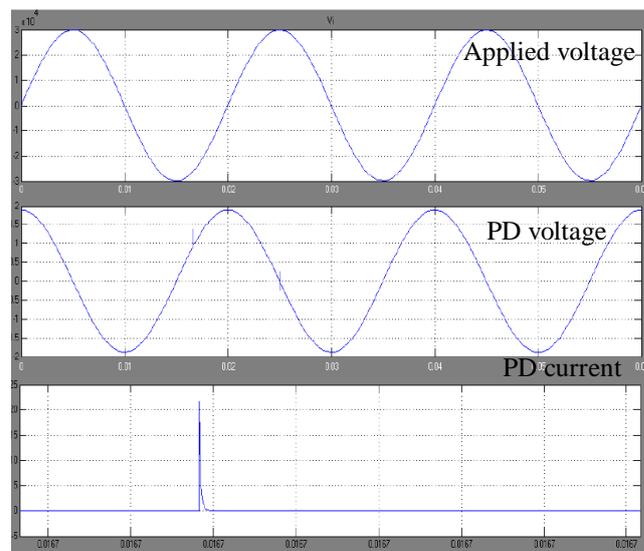
Applied Input Voltage (kV)	Current Discharge (A)
10	7.2
15	10.8
20	14.4
30	21.6



**Fig. 9. Result of Simulation of Applied Voltage 10kv.**



**Fig. 11. Result of simulation of applied voltage 20kV.**



**Fig. 12. Result of simulation of applied voltage 30kV.**

Fig. 10. Result of Simulation of Applied Voltage 15kv.

## VI.

### CONCLUSION

The simulation conducted showed that the extended PD equivalent circuit was able to represent the behaviour of PD in solid dielectrics. This circuit is more accurate because it considered the influence of local charge accumulations generated by preceding discharges.

There is a slight difference of voltage waveform and current discharges in the void from the original model. This is due to the timing mode of the breaker. Breakers cannot simulate the perfect timing for PD to occur. The breaker simulates the PD only once. The value of discharge current is dependent on the input voltage. If the input voltage is increased then the discharge current will increase.

The authors recommend mathematical modelling of the circuit operation as more manipulative efforts can be applied in further research work. The mathematical model can be base on the proposed from the extended PD equivalent circuit and simulated using MATLAB M-file application.

### ACKNOWLEDGMENT

The authors would like to thank Universiti Teknologi Malaysia (UTM) for the use of facilities to complete this research project. The authors would also like to thank Mr. W. M. Taufik and Mr. Novizon for their valuable advice, discussion, and help in completing this research work.

### REFERENCES

- [1] Kenroy Alexander Questelles, "Developing a Stochastic Model for Partial Discharge Detection In Voids of Polymeric Cable Insulation" University Technology Malaysia: Master Thesis, 2006.
- [2] Boggs, S.A. "Partial discharge: overview and signal generation", IEEE Electr. Insul. Mag., 1990, 6, (4), pp. 33-39.
- [3] A. L. Kupershtokh, C. P. Stamatelatos, and D. P. Agoris "Simulation of Partial Discharge Activity in Solid Dielectrics under AC Voltage" Vol. 32, No. 8, pp. 680-683. © Pleiades Publishing, Inc., 2006.
- [4] M. G. Danikas, G. E. Vassiliadis, "Models of Partial Discharges (PD) in Enclosed Cavities in Solid Dielectrics: A Study of The Relationship of PD Magnitudes to The Sensitivity of PD Detectors and Some Further Comments on Insulation Lifetime", Journal of Electrical Engineering, vol. 54, No. 5-6, pp. 132-135, 2003.
- [5] G. Chen, F. Baharudin, "Partial Discharge Modelling Based on a Cylindrical Model in Solid Dielectrics", International Conference on Condition Monitoring and Diagnosis, Beijing, China, pp. 1-5, Beijing, April 2008.
- [6] C.G. Karagiannopoulos, "A Model for Dielectrics Experiencing Partial Discharges under High Electric Fields", Journal of Electrostatics 65, pp. 535-541, 2007.

- [7] P. Das, S. Chakravorti, "Simulation of PD Patterns due to a Narrow Void in Different E-field Distribution", Journal of Electrostatics 68, pp. 218-226, 2010.
- [8] H. Illias, G. Chen, P. L. Lewin, "Partial Discharge Behavior within a Spherical Cavity in a Solid Dielectric Material as a Function of Frequency and Amplitude of the Applied Voltage", IEEE Transactions on Dielectrics and Electrical Insulation, vol. 18, No. 2, pp. 432-443, April 2011.
- [9] S. Ghosh, N.K. Kishore, "Modelling of Partial Discharge Inception and Extinction Voltages of Sheet Samples of Solid Insulating Materials using an Artificial Neural Network", IEE Proc.-Sci Meas. Technology, vol. 149, No. 2, pp. 73-78, March 2002.
- [10] Rainer Patsch and Martin Hoof "Physical Modelling of Partial Discharge Patterns" 1998 IEEE International Conference on Conduction and Breakdown in Solid Dielectrics, 1998.
- [11] Shampine, L. F., "Numerical Solution of Ordinary Differential Equations", Chapman & Hall, New York, 1994.

### AUTHOR BIOGRAPHY



**Yanuar Z. Arief** was born in Pontianak, Indonesia in 1971. He graduated from Department of Electrical Engineering, University of Tanjungpura, Pontianak, Indonesia in 1994. He received the M.S. degree from the Bandung Institute of Technology, Indonesia in 1998 and PhD from Kyushu Institute of Technology, Japan in 2006 and conducted a post doctoral research at Institute of Material & Diagnostic in Electrical Engineering, University of Siegen, Germany. Currently, he is a senior lecturer in Institute of High Voltage and High Current, Universiti Teknologi Malaysia, Johor Bahru, Malaysia. His research interest includes the partial discharge detection and degradation phenomena of polymeric insulating material, nanodielectric composite, renewable and biodegradable material as electrical insulation, and high voltage engineering insulation technology.



**Wan Akmal 'Izzati** was born in Johor Bahru, Malaysia in 1988. She obtained her Bachelor degree in Electrical Engineering from University Technology Malaysia in 2011 and currently pursuing Master degree at Institute of High Voltage and High Current, Universiti Teknologi Malaysia. Her research interest includes partial discharge and Nan dielectric composite as electrical insulating material.



**Zuraimy Adzis** was born in Singapore, in 1971. He graduated from University of Salford, Manchester in 1995. He received the M.Eng. Degree from the Universiti Teknologi Malaysia, in 2003. Currently, he is a lecturer in Institute of High Voltage and High Current, Universiti Teknologi Malaysia, Johor Bahru, Malaysia. His research interest includes EMC in high voltage Systems, with focus in lightning interaction and partial discharge phenomenon